

KEY ANSWERS

1	A	16	C	31	C	46	A
2	D	17	B	32	B	47	B
3	C	18	C	33	A	48	C
4	D	19	B	34	C	49	D
5	A	20	A	35	C	50	D
6	C	21	B	36	D	51	C
7	C	22	D	37	D	52	A
8	C	23	B	38	C	53	C
9	B	24	A	39	D	54	D
10	B	25	D	40	A	55	D
11	B	26	A	41	A	56	B
12	*	27	B	42	D	57	B
13	D	28	C	43	B	58	A
14	A	29	A	44	A	59	D
15	D	30	D	45	C	60	C

***: Grace mark**

1. Ten identical cells each emf 2V and internal resistance 1 Ω are connected in series with two cells wrongly connected. A resistor of 10 Ω connected to the combination. What is the current through the resistor?

A) 0.6 A B) 1.2 A C) 1.8 A D) 2.4 A **Ans. (A)**

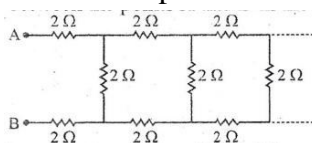
Solution : $\epsilon_{o,q} = 8 \times 2 - 2 \times 2 = 12 \text{ V}$

$$r_{e,q} = 10 \times 1 = 10 \Omega$$

$$R = 10 \Omega$$

$$I = \frac{\epsilon_{o,q}}{R_q + r} = \frac{12}{10 + 10} = 0.6 \text{ A}$$

2. The equivalent resistance between the points A and B in the following circuit is



A) 0.05 Ω B) 5 Ω C) 0.5 Ω D) 5.5 Ω **Ans. (D)**

Solution :

$$\left(\frac{x - 2}{x + 2} \right) + 4 = 5$$

$$\frac{x \times 2}{x + 2} + \frac{4}{1} = x$$

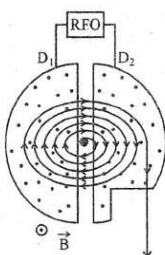
$$\frac{2x + 4x + 8}{x + 2} = x$$

$$6x + 8 = x^2 + 2x$$

$$x^2 - 4x - 8 = 0$$

$$\text{Solving } x = 5.5 \Omega$$

3. A charged particle is subjected to acceleration in a cyclotron as shown. The charged particle undergoes increase in its speed



A) Inside D₁, D₂ and the gaps B) Only inside D₁
C) Only in the gap between D₁ and D₂ D) only inside D₂ **Ans. (C)**

4. The resistance of a carbon resistor is $4.7 \text{ k}\Omega \pm 5\%$. The colour of the third band is
 A) violet B) orange C) gold D) red **Ans. (D)**

5. The four bands of a colour coded resistor are of the colours gray, red, gold and gold. The value of the resistance of the resistor is
 A) $8.2 \text{ k}\Omega \pm 5\%$ B) $82 \text{ k}\Omega \pm 5\%$ C) $5.2 \text{ k}\Omega \pm 5\%$. D) $82 \text{ k}\Omega \pm 10\%$. **Ans. (A)**

Solution : $8.2 \Omega \pm 5\%$

6. A wire of resistance R is connected across a cell of emf ϵ and internal resistance r. The current through the circuit is I. in the time t, the work done by the battery to establish the current I is

A) IRt B) I^2Rt C) ϵIt D) $\frac{\epsilon^2 t}{R}$ **Ans. (C)**

Solution : $\epsilon = \frac{W}{q} \Rightarrow \epsilon = \frac{W}{It} \Rightarrow W = \epsilon It$

7. For a given electric current the drift velocity of conduction electrons in a copper wire is v_d and their mobility is μ . When the current is increased at constant temperature

A) v_d decreases, μ remains the same B) v_d remains the same. μ decreases
 C) v_d increases, μ remains the same D) v_d remains the same, μ increases **Ans. (C)**

8. The torque acting on a magnetic dipole placed in uniform magnetic field is zero, when the angle between the dipole axis and the magnetic field is _____.

A) 60° B) 90° C) zero D) 45° **Ans. (C)**

Solution : $\tau = MB \sin \theta$

$$\epsilon = \frac{W}{q} \Rightarrow \epsilon = \frac{W}{It} \Rightarrow W = \epsilon It$$

9. The horizontal component of Earth's magnetic field at a place is $3 \times 10^{-5} \text{ T}$. if the dip at that place is 45° , the resultant magnetic field at that place is

A) $\frac{3}{2}\sqrt{3} \times 10^{-5} \text{ T}$ B) $3\sqrt{2} \times 10^{-5} \text{ T}$ C) $3 \times 10^{-5} \text{ T}$ D) $\frac{3}{\sqrt{2}} \times 10^{-5} \text{ T}$ **Ans. (B)**

Solution : $B_\mu = B_E \text{ csc } \theta$

$$3 \times 10^{-5} = B_E \text{ csc } 45^\circ$$

$$B_E = 3\sqrt{2} \times 10^{-5} \text{ T}$$

10. Proton and an alpha-particle moving with the same velocity enter a uniform magnetic field with their velocities perpendicular to the magnetic field. The ratio of radii of their circular paths is

A) 4 : 1 B) 1 : 2 C) 2 : 1 D) 1 : 4 **Ans. (B)**

Solution : $r = \frac{mv}{qB} \Rightarrow r \propto \frac{m}{q}$

$$\frac{r_p}{r_\alpha} = \frac{m_p}{m_\alpha} \times \frac{q_\alpha}{q_p} \Rightarrow \frac{r_p}{r_\alpha} = \frac{1}{4} \times \frac{2}{1} = \frac{1}{2}$$

11. A moving coil galvanometer is converted into an ammeter of range 0 to 5 mA. The galvanometer resistance is 90Ω and the shunt resistance has a value of 10Ω . If there are 50 divisions in the galvanometer-turned-ammeter on either sides of zero, its current sensitivity is

A) $2 \times 10^4 \text{ A/div}$ B) $1 \times 10^5 \text{ div/A}$ C) $2 \times 10^4 \text{ div/A}$ D) $1 \times 10^5 \text{ A/div}$ **Ans. (B)**

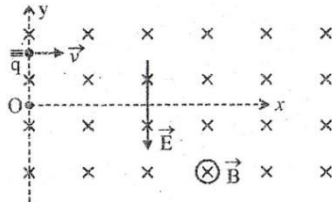
Solution : $R_s = \frac{R_G}{n - 1}$

$$10 = \frac{90}{n - 1} \Rightarrow n = 10$$

$$\text{Current range of galvanometer} = \frac{5\text{mA}}{10} = 5 \times 10^{-4} \text{ A}$$

$$\text{Sensitivity} = \frac{50}{5 \times 10^{-4}} = 1 \times 10^5 \text{ div / A}$$

12. A positively charged particle of mass m is passed through a velocity selector. It moves horizontally rightward without deviation along the line $y = \frac{2mv}{qB}$ with a speed v . The electric field is vertically downwards and magnetic field is into the plane of the paper. Now, the electric field is switched off at $t = 0$. The angular momentum of the charged particle about origin O at $t = \frac{\pi m}{qB}$ is



- A) zero B) $\frac{mE^3}{qB^2}$ C) $\frac{mE^2}{qB^3}$ D) $\frac{2mE^2}{qB^3}$ **Ans. (*)**

Solution : Ambiguous Question
Seems to have wrong options

13. The Curie temperatures of Cobalt and iron are 1400 K and 100 K respectively. At $T = 1600$ K, the ratio of magnetic susceptibility of Cobalt to that of iron is
- A) $\frac{7}{5}$ B) $\frac{5}{7}$ C) $\frac{1}{3}$ D) 3 **Ans. (D)**

Solution : $\chi = \frac{C}{T - T_C}$

$$\frac{\chi_{Co}}{\chi_{Fe}} = \frac{(T - T_C)_{Fe}}{(T - T_C)_{Co}}$$

$$\frac{\chi_{Co}}{\chi_{Fe}} = \left(\frac{1600 - 1000}{1600 - 1400} \right) = 3$$

14. An ideal transformer has a turns ratio of 10. When the primary is connected to 220 V, 50 Hz ac source, the power output is
- A) equal to power input B) zero
C) 10 times the power input D) $\frac{1}{10}$ the power input **Ans. (A)**

Solution : Since it is an ideal transformer.

15. The current in a coil changes from 2A to 5A in 0.3 s. The magnitude of emf induced in the coil is 1.0 V. The value of self-inductance of the coil is
- A) 0.1 mH B) 10 mH C) 1.0 mH D) 100 mH **Ans. (D)**

Solution : $\varepsilon = -L \frac{di}{dt}$

$$1 = -L \frac{(5 - 2)}{0.3}$$

$$L = \frac{0.3}{3} = 0.1 = 100 \text{ mH}$$

16. A metallic rod of length 1m held along east-west direction is allowed to fall down freely. Given horizontal component of earth's magnetic field $B_H = 3 \times 10^{-5}$ T. The emf induced in the rod at an instant $t = 2$ s after it is released is (Take $g = 10 \text{ ms}^{-2}$)
- A) 3×10^{-4} V B) 6×10^{-3} V C) 6×10^{-4} V D) 3×10^{-3} V **Ans. (C)**

Solution : $\varepsilon = Blv$

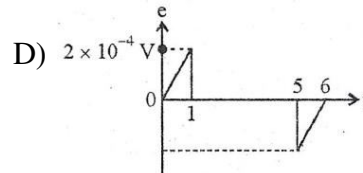
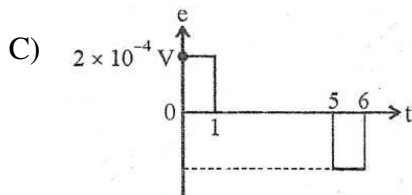
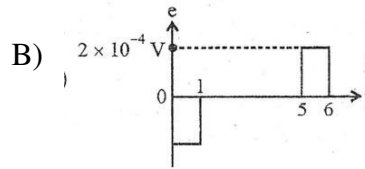
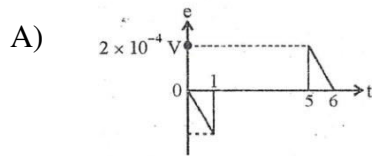
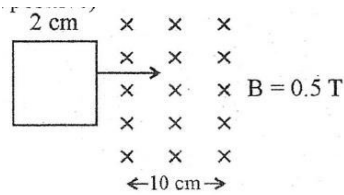
$$= 3 \times 10^{-5} \times 1 \times 20$$

$$\because v = u + at$$

$$= 60 \times 10^{-5} \text{ V} = 6 \times 10^{-4} \text{ V}$$

$$v = 0 + 10 \times 2 = 20 \text{ ms}^{-1}$$

17. A square loop of side 2 cm enters a magnetic field with a constant speed of 2 cm s^{-1} as shown. The front edge enters the field at $t = 0$ s. Which of the following graph correctly depicts the induced emf in the loop? (Take clockwise direction positive)



Ans. (B)

Solution: $\varepsilon = \text{const}$

From $t = 0$ to $t = 1$ (negative and constant)

$t = 1$ to $t = 5$ (zero)

$t = 5$ to $t = 6$ (positive and constant)

18. In series LCR circuit at resonance, the phase difference between voltage and current is

A) $\frac{\pi}{4}$

B) $\frac{\pi}{2}$

C) zero

D) π

Ans. (C)

Solution : Zero

19. An equiconvex lens made of glass of refractive index $\frac{3}{2}$ has focal length f in air. It is completely immersed in water of refractive index $\frac{4}{3}$. The percentage change in the focal length is

A) 400% decrease

B) 300% increase

C) 400% increase

D) 300% decrease

Ans. (B)

Solution : $\tan = f$

$$f_w = 4f$$

$$\text{Percentage change} = \left(\frac{4f - f}{f} \right) 100 = 300\% \text{ increase}$$

20. A point object is moving at a constant speed of 1 ms^{-1} along the principal axis of a convex lens of focal length 10 cm. The speed of the image is also 1 ms^{-1} , when the object is _____ cm from the optic centre of lens.

A) 20

B) 5

C) 10

D) 15

Ans. (A)

Solution : $\vec{V}_{IL} = m^2 \vec{V}_{OL}$

$$1 = \left(\frac{f}{f+u} \right)^2 \times (-1)$$

$$u = 20 \text{ cm}$$

$$\left(\frac{10}{10+u} \right)^2 = -1 \Rightarrow \frac{10}{10+u} = 1 \Rightarrow -10 = -10+u$$

21. When light propagates through a given homogeneous medium, the velocities of

A) primary wavefronts are greater than or equal to those secondary wavelets.

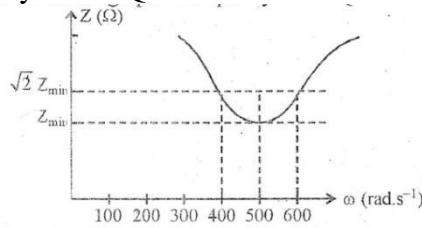
B) primary wavefronts wavelets are equal.

C) primary wavefronts are larger than those of secondary wavelets.

D) primary wavefronts are lesser than those secondary wavelets.

Ans. (B)

22. Total impedance of a series LCR circuit varies with angular frequency of the AC source connected to it as shown in the graph. The quality factor Q of the series LCR circuit is



- A) 5 B) 1 C) 0.4 D) 2.5 **Ans. (D)**

Solution : $Q = \frac{\omega_0}{2\Delta\omega} = \frac{500}{200} = 2.5$

23. The ratio of the magnitudes of electric field to the magnetic field of an electromagnetic wave is of the order of

- A) 10^{-5} ms^{-1} B) 10^8 ms^{-1} C) 10^{-8} ms^{-1} D) 10^5 ms^{-1} **Ans. (B)**

Solution : $\because C = \frac{E}{B} \Rightarrow C = 3 \times 10^8$

24. For a point object, which of the following always produces virtual image in air?

- A) Convex mirror B) Biconvex lens C) Concave mirror D) Plano-convex lens **Ans. (A)**

25. For a given pair of transparent media, the critical angle for which colour is maximum?

- A) Blue B) Violet C) Green D) Red **Ans. (D)**

Solution : n_R is least

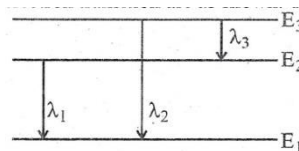
$\sin C_R = \frac{1}{n_R} \Rightarrow C_R$ is highest

26. In the Rutherford's alpha scattering experiment, as the impact parameter increases the scattering angle of the alpha particle

- A) Decreases B) Increases C) remains the same D) is always 90 **Ans. (A)**

Solution : Decreases

27. Three energy levels of hydrogen atom and the corresponding wavelength of the emitted radiation due to different electron transition are as shown. Then,



- A) $\lambda_2 = \lambda_1 + \lambda_3$ B) $\lambda_2 = \frac{\lambda_1 \lambda_3}{\lambda_1 + \lambda_3}$ C) $\lambda_3 = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$ D) $\lambda_1 = \frac{\lambda_2 \lambda_3}{\lambda_2 + \lambda_3}$ **Ans. (B)**

Solution : $\frac{hc}{\lambda_1} + \frac{hc}{\lambda_3} = \frac{hc}{\lambda_2}$

$\frac{1}{\lambda_1} + \frac{1}{\lambda_3} = \frac{1}{\lambda_2}$

$\lambda_2 = \frac{\lambda_1 \lambda_3}{\lambda_1 + \lambda_3}$

28. An unpolarised light of intensity I is passed through two polaroids kept one after the other with their planes parallel to each other. The intensity of light emerging from second Polaroid is $\frac{1}{4}$. The angle between the pass axes of the polaroids is

- A) 60° B) 30° C) 45° D) 0° **Ans. (C)**

Solution : $I = I_0 \cos^2(\theta)$

$$\frac{I}{4} = \frac{I_0}{2} \cos^2(\theta)$$

$$\frac{1}{2} = \cos^2 \theta$$

$$\cos \theta = \frac{1}{2}, \theta = 45^\circ$$

29. In the Young's double slit experiment, the intensity of light passing through each of the two slits is $2 \times 10^{-2} \text{ Wm}^{-2}$. The screen-slit distance is very large in comparison with slit-slit distance. The fringe width is β . The distance between central maximum and a point P on the screen is $x = \frac{\beta}{3}$. Then the total light intensity at that point is

- A) $2 \times 10^{-2} \text{ Wm}^{-2}$ B) $16 \times 10^{-2} \text{ Wm}^{-2}$ C) $8 \times 10^{-2} \text{ Wm}^{-2}$ D) $4 \times 10^{-2} \text{ Wm}^{-2}$ **Ans. (A)**

Solution :

$$I_R = 4I_0 \cos^2\left(\frac{\phi}{2}\right)$$

$$= 4 \times 2 \times 10^{-2} \cos^2 60^\circ$$

$$= 2 \times 10^{-2} \text{ W/m}^2$$

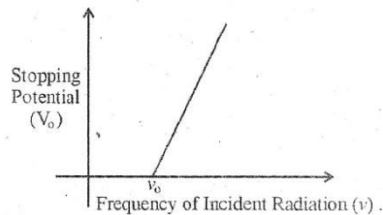
$$\left. \begin{array}{l} \text{Path diff} = \frac{xd}{D} \\ \Delta = \frac{\beta d}{3D} = \frac{\lambda D}{3d} \cdot \frac{d}{D} = \frac{\lambda}{3} \\ \phi = \frac{2\pi}{\lambda} \Delta = \frac{2\pi}{3} = 120^\circ \end{array} \right\}$$

30. A 60 W source emits monochromatic light of wavelengths 662.5 nm. The number of photons emitted per second is
- A) 5×10^{26} B) 2×10^{29} C) 5×10^{17} D) 2×10^{20} **Ans. (D)**

Solution : $P = n \frac{hc}{\lambda}$

$$n = \frac{P\lambda}{hc} = \frac{60 \times 662.5 \times 10^{-9}}{20 \times 10^{-20}} = 2000 \times 10^{17} = 2 \times 10^{20}$$

31. In an experiment to study photo- electric effect the observed variation of stopping potential with frequency of incident radiation with frequency of incident radiation is as shown in the figure. The slope y – intercept are respectively



- A) $\frac{hv}{e}, -\frac{h}{e}$ B) $hv, -hv_0$ C) $\frac{h}{e}, -\frac{hv_0}{e}$ D) $\frac{hv}{e}, v_0$ **Ans. (C)**

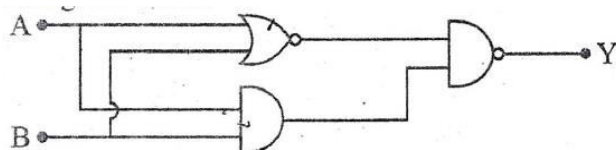
Solution : slope = $\frac{h}{e}$

$$y\text{-int except} = \frac{-hv_0}{e}$$

32. A full-wave rectifier with diodes D_1 and D_2 is used to rectify 50 Hz alternating voltage. The diode D_1 conducts _____
- A) 75 B) 50 C) 100 D) 25 **Ans. (B)**

Solution : In FWR single diode conducts 50 times in one second

33. The truth table for the given circuit is



(A)	A	B	Y	(B)	A	B	Y	(C)	A	B	Y	(D)	A	B	Y
	1	1	1		1	1	1		1	1	1		1	1	1
	1	0	1		1	0	1		1	0	1		1	0	0
	0	1	1		0	1	1		0	1	0		0	1	1
	0	0	1		0	0	0		0	0	1		0	0	1

Ans. (A)

34. The energy gap of an LED is 2.4 eV. When the Led is witched 'ON', the momentum of the emitted photons is

A) $1.28 \times 10^{-11} \text{ kg.m.s}^{-1}$

B) $0.64 \times 10^{-27} \text{ kg.m.s}^{-1}$

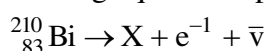
C) $1.28 \times 10^{-27} \text{ kg.m.s}^{-1}$

D) $2.56 \times 10^{-27} \text{ kg.m.s}^{-1}$

Ans. (C)

Solution : $P = \frac{E}{C} = \frac{2.4 \times 1.6 \times 10^{-19}}{3 \times 10^8} = 1.28 \times 10^{-27} \text{ kg / ms}^{-1}$

35. In the following equation representing β^- decay the number of neutrons in the nucleus X is



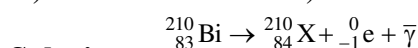
A) 125

B) 84

C) 126

D) 127

Ans. (C)



Number of neutrons = $210 - 84 = 126$

36. A nucleus with mass number 220 initially at rest emits an alpha particle, if the Q value of reaction is 5.5 MeV, calculate the value of kinetic energy of alpha particle.

A) 7.4 MeV

B) 4.5 MeV

C) 6.5 MeV

D) 5.4 MeV

Ans. (D)

Solution : $K_{\alpha} = \frac{A-4}{A} \times Q$

$$= \frac{216}{220} \times 5.5$$

$$= 5.4 \text{ MeV}$$

37. A radioactive sample has half-life of 3 years. The time required for the activity of the sample to reduce to $\frac{1}{5}$ its initial values is about

A) 15 years

B) 5 years

C) 10 years

D) 7 years

Ans. (D)

Solution : $\frac{1}{5}$ of initial value = 20 %

This should be between 2 half lives and 3 half lives. Answer between 6 days and 9 days

38. When a p-n junction diode is in forward bias, which type of charge carriers flows in the connecting wire?

A) Protons

B) Holes

C) Free electrons

D) Ions

Ans. (C)

Solution :

39. A ball of mass 0.2 kg is thrown vertically down form a height of 10 m. it collides with the floor and loses 50% of its energy and then rises back to the same height. The value of its initial velocity is

A) 196 ms^{-1}

B) 20 ms^{-1}

C) zero

D) 14 ms^{-1}

Ans. (D)

Solution : Initially

$$TE = \frac{1}{2} mV^2 + mgh$$

After bouncing back

$$TE = \frac{1}{2} \left(\frac{1}{2} mV^2 + mgh \right)$$

At the highest point

$$TE = \frac{1}{2} \left(\frac{1}{2} mV^2 + mgh \right) = mgh$$

$$\frac{1}{4} mV^2 + \frac{mgh}{2} = mgh$$

$$\frac{1}{4} V^2 = \frac{gH}{2}$$

$$V^2 = 2gh = 2 \times 9.8 \times 10$$

$$V^2 = 196 \Rightarrow V = 14 \text{ ms}^{-1}$$

40. The moment of inertia of a rigid body about an axis

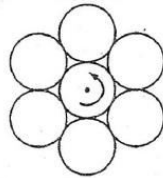
A) depends on the position of axis of rotation. B) does not depend on its size.

C) does not depend on its mass.

D) does not depend on its shape.

Ans. (A)

41. Seven identical discs are arranged in a planar pattern, so as to touch each other as shown in the figure. Each disc has mass 'm' radius R. what is the moment of inertia of system of six discs about an axis passing through the centre of central disc and normal to plane of all discs?



A) $\frac{55 mR^2}{2}$

B) $\frac{85 mR^2}{2}$

C) $27 mR^2$

D) $10027 mR^2$

Ans. (A)

Solution: $I = I_{\text{centre}} + (\text{M.I of surrounding discs})$

$$= \frac{mR^2}{2} + \left(6 \frac{mR^2}{2} + 6m(2R)^2 \right) = \frac{55mR^2}{2}$$

42. The true length of a wire is 3.678 cm. when the length of this wire is measure instrument A, the length of the wire is 3.5 cm. When the length of the wire is measured using instrument B, it is found to have length 3.38 cm. Then the

A) measurement with B is more accurate and precise.

B) measurement with A is more precise while measurement with B is more accurate.

C) measurement with A is more accurate and precise.

D) measurement with A is more accurate while measurement with B is more precise.

Ans. (D)

43. A body is moving along a straight line with initial velocity v_0 . Its acceleration a is constant. After t seconds, its velocity becomes v. the average velocity of the body over the given time interval is

A) $\bar{v} = \frac{v^2 + v_0^2}{2at}$

B) $\bar{v} = \frac{v^2 - v_0^2}{2at}$

C) $\bar{v} = \frac{v^2 - v_0^2}{at}$

D) $\bar{v} = \frac{v^2 + v_0^2}{2at}$

Ans. (B)

Solution: $V^2 - V_0^2 = 2as$

$$S = \frac{V^2 - V_0^2}{2a}$$

$$\text{Average velocity} = \frac{V^2 - V_0^2}{2at} \left(= \frac{\text{displacement}}{\text{time}} \right)$$

44. A particle is in uniform circular motion. Related to one complete revolution of the particle, which among the statements is incorrect?

A) Average speed of the particle is zero

B) Average velocity of the particle is zero

C) Average acceleration of the particle is zero

D) Displacement of the particle is zero

Ans. (A)

45. A body of mass 10 kg is kept on a horizontal surface, the coefficient of kinetic friction between the body and the surface is 0.5. A horizontal force of 60 N is applied on the body. The resulting acceleration of the body is about

A) 6 ms^{-2}

B) zero

C) 1 ms^{-2}

D) 5 ms^{-2}

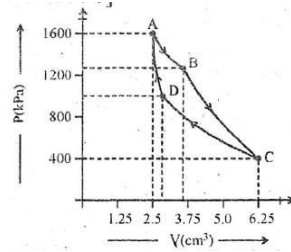
Ans. (C)

Solution: $F_{\text{net}} = F - \mu_k N$

$$10 a = 60 - 0.5 \times 10 \times 10$$

$$A = 1 \text{ ms}^2$$

46. The P-V diagram of a Carnot's engine is shown in the graph below. The engine uses 1 mole of an ideal gas as working substance. From the graph, the area enclosed by the P-V diagram is [The heat supplied to the gas is 8000J]



- A) 3000 J B) 1000 J C) 1200 J D) 2000 J

Ans. (A)

Solution: For AB,

$$PV = nRT$$

$$1600 \times 10^3 \times 2.5 \times 10^{-6} = 1 \times R \cdot T$$

$$T = \frac{4}{R}$$

CD is isothermal

$$P_o V_o = nRT^1$$

$$400 \times 10^3 \times 6.5 \times 10^{-6} = 1 \times R \times T^1$$

$$T^1 = \frac{2.5}{R} \text{ K}$$

$$\eta = 1 - \frac{2.5R}{4R} = 0.375$$

$$\omega = \eta Q = 0.375 \times 8000 = 3000 \text{ J}$$

47. When a planet revolves around the sun, in general, for the planet

- A) kinetic and potential energy of the planet are constant.
 B) angular momentum about the Sun and aerial velocity of the planet are constant.
 C) linear momentum and linear velocity are constant.
 D) linear momentum and aerial velocity are constant.

Ans. (B)

48. A stretched wire of a material whose Young's modulus $Y = 2 \times 10^{11} \text{ Nm}^{-2}$ has Poisson's ratio 0.25. its lateral strain $\epsilon_l = 10^{-3}$. The elastic energy density of the wire is

- A) $4 \times 10^5 \text{ Jms}^{-3}$ B) $8 \times 10^5 \text{ Jms}^{-3}$ C) $16 \times 10^5 \text{ Jms}^{-3}$ D) $1 \times 10^5 \text{ Jms}^{-3}$

Ans. (C)

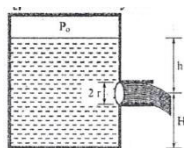
Solution: Poisson's ratio = $\frac{\text{lateral strain}}{\text{consitudinal strain}}$

$$\text{logitudenal strain} = \frac{\text{lateral strain}}{\text{poissains ratio}} = \frac{10^{-3}}{0.25} = 4 \times 10^{-3}$$

$$\text{Energy density} = \frac{1}{2} Y \text{ strain}^2 = \frac{1}{2} \times 2 \times 10^{16} \times (4 \times 10^{-3})^2 = 16 \times 10^5 \text{ Jm}^{-3}$$

49. A closed water tank has cross-sectional area A . It has a small hole at a depth of h from the free surface

of water. The radius of the hole is r so that $r \ll \sqrt{\frac{A}{\pi}}$. If P_o is the pressure inside the tank above water level, and P_a is the atmospheric pressure, the rate of flow of the water coming out of the hole is [ρ is the density of water]



- A) $\pi r^2 \sqrt{2gh}$ B) $\pi r^2 \sqrt{gh + \frac{2(P_o - P_a)}{\rho}}$ C) $\pi r^2 \sqrt{2gh}$ D) $\pi r^2 \sqrt{2gh + \frac{2(P_o - P_a)}{\rho}}$

Ans. (D)

Solution: $V = \sqrt{2gh + 2\left(\frac{P_o - P_a}{\rho}\right)}$

According to equation of continuity $AV = \pi r^2 \sqrt{2gh + \frac{2(P_o - P_a)}{\rho}}$

50. 100 g of ice at 0 °C is mixed with 100 g of water at 100 °C. The final temperature of the mixture is

[Take $L_f = 3.36 \times 10^5 \text{ J kg}^{-1}$ and $S_w = 4.2 \times 10^3 \text{ J kg}^{-1} \text{ K}^{-1}$]

- A) 50 °C B) 1 °C C) 40 °C D) 10 °C **Ans. (D)**

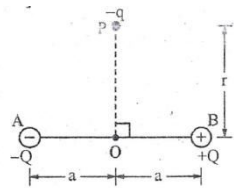
Solution:

$$mL_f + mC_w(T - 0) = mC_w(100 - T)$$

$$100 \times 80 + 100 \times 1(T) = 100 \times 1 \times (100 - T)$$

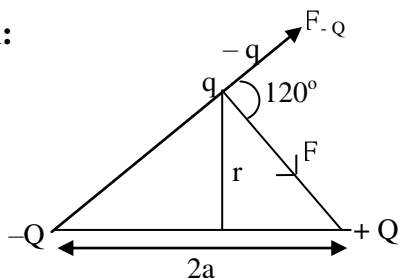
$$T = 10^\circ\text{C}$$

51. In the situation shown in the diagram, magnitude of $q \ll |Q|$ and $r \gg a$. The net force and the net torque on it about O at the instant shown are respectively [$p = 2aQ$ is the dipole moment]



- A) $-\frac{1}{4\pi\epsilon_0} \frac{pq}{r^2} \hat{k}, -\frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} \hat{i}$ B) $\frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} \hat{i}, +\frac{1}{4\pi\epsilon_0} \frac{pq}{r^2} \hat{k}$
- C) $\frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} \hat{i}, -\frac{1}{4\pi\epsilon_0} \frac{pq}{r^2} \hat{k}$ D) $\frac{1}{4\pi\epsilon_0} \frac{pq}{r^2} \hat{k}, \frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} \hat{i}$ **Ans. (C)**

Solution:



$$\vec{F} = -q\vec{E}$$

$$= -q \frac{KQ}{r^3} (-\hat{i}) = k \frac{PQ}{r^3} (\hat{i}) = \frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} (\hat{i})$$

$$\vec{\tau} = \vec{r} \times \frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} (\hat{i}) = \frac{1}{4\pi\epsilon_0} \frac{pq}{r^3} (-\hat{k})$$

52. Pressure of ideal gas at constant volume is proportional to
 (A) total energy of the gas (B) average kinetic energy of the molecules
 (C) force between the molecules (D) average potential energy of the molecules **Ans. (A)**

Solution: * P is directly proportional to total internal energy of gas.

53. A block of mass m is connected to a light spring of force constant k. The system is placed inside a damping medium of damping constant b. The instantaneous values of displacement x, acceleration a and energy E respectively. The initial amplitude of oscillation is A and ω' is the angular frequency of oscillations. The incorrect expression related to the damped oscillations is

- A) $E = \frac{1}{2} kA^2 e^{-\frac{bt}{m}}$ B) $m \frac{d^2x}{dt^2} + b \frac{dx}{dt} + kx = 0$
- C) $x = Ae^{-\frac{b}{m}t} \cos(\omega't + \phi)$ D) $\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$ **Ans. (C)**

54. The speed of sound in an ideal gas at a given temperature T is v. The rms speed of gas molecules at that temperature is v_{rms} . The ratio of the velocities v and v_{rms} for helium and oxygen gases are X and X' respectively. Then $\frac{X}{X'}$ is equal to

- A) $\sqrt{\frac{5}{21}}$ B) $\frac{21}{5}$ C) $\frac{21}{\sqrt{5}}$ D) $\frac{5}{\sqrt{21}}$ **Ans. (D)**

Solution: $V = \sqrt{\frac{\gamma RT}{M}} \Rightarrow v_{rms} = \sqrt{\frac{3RT}{M}}$

$$X = \frac{V}{v_{rms}} = \sqrt{\frac{\gamma}{3}}$$

$$\frac{X}{X'} = \sqrt{\frac{r_{me}}{r_{o2}}} = \sqrt{\frac{3}{7}} = \frac{5}{\sqrt{21}}$$

55. A positively charged glass rod is brought near uncharged metal sphere, which is mounted on an insulated stand. If the glass rod is removed, the net charge on the metal sphere is

- A) 1.6×10^6 C B) Positive charge C) Negative charge D) Zero **Ans. (D)**

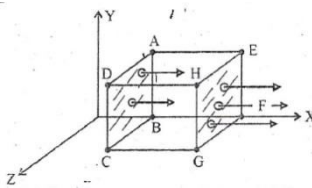
56. A parallel plate capacitor of capacitance C_1 with a dielectric slab in between its plates is connected to a battery. It has a potential difference V_1 across its plates. When the dielectric slab is removed, keeping the capacitor connected to the battery, the new capacitance Potential difference are C_2 and V_2 respectively. Then,

- A) $V_1 < V_2, C_1 > C_2$ B) $V_1 = V_2, C_1 > C_2$ C) $V_1 = V_2, C_1 < C_2$ D) $V_1 > V_2, C_1 > C_2$ **Ans. (B)**

Solution: $C_1 > C_2$ and $V_1 = V_2$

57. A cubical Gaussian surface has side of length $a = 10$ cm. Electric field lines are parallel to x-axis as shown. The magnitudes of electric fields through surfaces ABCD and EFGH 6 kNC^{-1} and 9 kNC^{-1} respectively. Then the total charge enclosed by the cube is

[Take $\epsilon_0 = 9 \times 10^{-12} \text{ Fm}^{-1}$]



- A) -1.35 nC (B) 0.27 nC C) -0.27 nC D) 1.35 nC **Ans. (B)**

Solution: $\phi_{ABCD} = EA \cos \theta$

$$= 6 \times 10^3 (10 \times 10^{-2})^2 \cos 180^\circ = -60 \text{ V}_m \text{ (inward flux)}$$

Similarly: $\phi_{EFGH} = 9 \times 10^3 (10 \times 10^{-2})^2 \cos 0^\circ$

$$= 90 \text{ V}_m \text{ (outward flux)}$$

$$\phi_{\text{total}} = 30 \text{ V}_m$$

$$Q = \epsilon_0 \phi$$

$$= 9 \times 10^{-12} \times 30$$

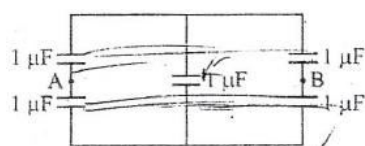
$$= 270 \times 10^{-12} = 0.27 \text{ nC}$$

58. Electric field at a distance 'r' from an infinitely long uniformly charged straight conductor having linear charge density λ . is E_1 . Another uniformly charged conductor having same linear charge density λ is bent into a semicircle of radius 'r'. The electric field at its centre E_2 . Then

- (A) $E_1 = E_2$ (B) $E_1 = \pi r E_2$ (C) $E_2 = \pi r E_1$ (D) $E_2 = \frac{E_1}{r}$ **Ans. (A)**

Solution: $E_1 = E_2 = \frac{\lambda}{2\pi\epsilon_0 r}$

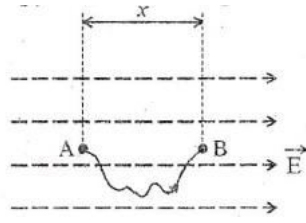
59. Five capacitors each of value $1 \mu\text{F}$ are connected as shown in the figure The equivalent capacitance between A and B is



- (A) $2 \mu\text{F}$ B) $5 \mu\text{F}$ (C) $3 \mu\text{F}$ (D) $1 \mu\text{F}$ **Ans. (D)**

Solution: Balanced Wheatstones network

60. A uniform electric field vector \vec{E} exists along horizontal direction as shown. The electric potential at A is V_A . A small point charge q is slowly taken from A to B along the curved path as shown. The potential energy of the charge when it is at point B is



(A) $q[Ex - V_A]$

(B)

qEx

(C) $q[V_A - Ex]$

Solution: $V_A - V_B = Ex$

$$V_B = V_A - Ex$$

$$U_B = qV_B$$

$$U_B = q(V_A - Ex)$$